# %Chapter Fundmental Knowledge

%introduction

Before the discussion about coupling fibers to waveguides it is necessary to present some basic knowledge involved in this work. In this chapter lens theory and fiber optics will be as common knowledge at first introduced. Then the description of Gaussian beam is helpful for understanding some terms, such as spot size, in the following research.

In order to analyze the simulations results from CST MWS, we also have to present finite integral method (FIT), which is implemented in CTS MWS. At last in this work S-Parameters will be described in this chapter because the $|S\_{21}|$ is generally used to measure the coupling efficiency.

## %\section{Optics}

### \subsectioin{Lens Theory}

%Lens optics

Lens is widely applied in optics. Some are used for photography of camera; some are used for microscopes and telescopes. In this work lens is used for coupling fibers to photonic waveguide. No matter what kind of application they all base on primary rules: lens theory.\\

One important function of lens is focus. It is a common experience by using a magnifying glass to set small pieces of paper or leaves on fire with sunlight. In this scene the lens of the magnifying glass focuses all incoming sun rays at a single spot. This spot is called focal point and the distance between the focal point and the center of the lens is called focal length $f$. The dimensions of this spot and the focal length are two primary characters of the lens and values of them depend on the radium of curvature of the lens surface and on the refractive index of the material the lens is made from. \\

\begin{figure}[httbp]

\centering

\includegraphics[width=0.6\textwidth]{bilder/lens\_define}

\caption{The quantities define of singlet lenses \cite{lens\_theory\_LC\_Ltd}}

\label{fig:lens\_define}

\end{figure}

In order to understand more specifics about lenses Fig.\ref{fig:lens\_define} presents a singlet lens with geometric parameters. \”The optical axis (O-O')of the lens is a line passing through the centers of curvature of the two spherical lens surfaces. \”

Rays A and B, parallel with the optic axis (O-O'), are casted from different two sides through the lens and respectively cross the axis at their front and back focal points $F1$ and $F2$. The front and back principal points $H1$ and $H2$ are the intersections of the optical axis with the front and back principal surfaces. Points $V1$ and $V2$ are called the front and back vertices respectively\cite{lens\_theory\_LC\_Ltd}. Some important quantities are defined in Tab. \ref{tab:lens\_quantities}. Here the distance $t\_{c}$ is the center thickness of the lens $V1V2$.\\

\begin{table}

\centering

\caption{Important Quantities for Singlet Lenses Immersed in Air \cite{lens\_theory\_LC\_Ltd}}

\begin{tabular}{|c|c|c|}

\hline

\textbf{Symbol}&\textbf{Description}&\textbf{Formular}\\

\hline

$f$ & \parbox[c]{6cm}{

\begin{center}

effective focal length

\end{center}

}& $\frac{1}{f}=(n-1)\left[\frac{1}{R\_{1}}-\frac{1}{R\_{2}} \right]+\frac{t\_{c}(n-1)^2}{nR\_{1}R\_{2}}$ \\

\hline

$BFD$ &\parbox[c]{6cm}{

\begin{center}

back focal distance

\end{center}

}& $BFD=f\left[ 1-\frac{t\_{c}(n-1)}{nR\_{1}}\right]$ \\

\hline

$FFD$ &\parbox[c]{6cm}{

\begin{center}

front focal distance

\end{center}

}& $FFD=f\left[ 1+\frac{t\_{c}(n-1)}{nR\_{1}}\right]$ \\

\hline

$H2V2$ & \parbox[c]{6cm}{

\begin{center}

back vertex to back principal point distance

\end{center}

} & $H\_{2}V\_{2}=f-BFD=-f\frac{t\_{c}(n-1)}{nR\_{1}}$ \\

\hline

$V1H1$ & \parbox[c]{6cm}{

\begin{center}

front vertex to front principal point distance

\end{center}

} & $V\_{1}H\_{1}=f-FFD=-f\frac{t\_{c}(n-1)}{nR\_{2}}$ \\

\hline

\end{tabular}

\label{tab:lens\_quantities}

\end{table}

The classical singlet lenses are plano convex, plano concave, equiconvex and equiconcave lenses, which are listed in following Tab.\ref{tab:lenses\_focal\_length} with their focal length relation.\\

\begin{table}

\begin{tabular}{|c|c|c|}

\hline

\textbf{Type}&\textbf{Description}&\textbf{Formular}\\

\hline

Plano Convex & \parbox[c]{2.1cm}{\includegraphics[width=2cm]{bilder/plano\_convex}}& $f=\frac{R}{(n-1)}$ \\

\hline

Plano Concave &\parbox[c]{2.1cm}{\includegraphics[width=2cm]{bilder/plano\_concave}} & $f=-\frac{R}{(n-1)}$ \\

\hline

Equiconvex & \parbox[c]{2.1cm}{\includegraphics[width=2cm]{bilder/equi\_convex}} & $f=\left[\frac{2(n-1)}{R} - \frac{t\_{c}(n-1)^2}{nR^2}\right]^{-1}$ \\

\hline

Equiconcave & \parbox[c]{2.1cm}{\includegraphics[width=2cm]{bilder/equi\_concave}} & $f=\left[\frac{2(n-1)}{R} + \frac{t\_{c}(n-1)^2}{nR^2}\right]^{-1}$ \\

\hline

\end{tabular}

\caption{Focal length Formulas of Simple Singlet Lenses in Air.

The Radii are considered positive in the formulas below.}

\label{tab:lenses\_focal\_length}

\end{table}

The performance of a lens is usually estimated by spot size and focal lengths. The definition of the spot size will be declared later in section \ref{sect:gaussian\_beam}. The focal length is in common sense the distance from lens center to minimum spot. But this idea is not exact in any case.

Spot size,which introduced in section \textbf{Gaussian Beam}, is also a important quality of a lens. The smaller minimum spot size a lens has, the stronger focusing ability it has. For a small angle lens the smallest spot locate approxmiately at its focus. But for a wide angle lens it is a different case.

\cite{lens\_theory\_LC\_Ltd} has refer that the minimu Spot lies between the maeginal plane and paraxial focal plane. Fig.\ref{fig:min\_max\_spot} is a "'geometrical trace of 25 rays in the focal region 100mm focal length BK7 plano convex lens(n=1.515)."' All the distances which are in following discussed base on the assumption that the back vertex (V2) of the lens are regarded as origin(0 point). The rays are launched parallel to the axis(O-O') and equally spaced in a region above and below the axis in a plane containing the axis(\textbf{meridional plane}). Therefor, the lens is operating at the rahter "`faster"' aperture of f/3.125. The marginal rays reach the axis first,in plane \textbf{MP}. The paraxial rays reach the axis lasr, at the \textbf{paraxial focal plane}(\textbf{PP}). The Distance from \textbf{V2} to \textbf{PP} is the back focal distance (\textbf{BFD}) of the lens. This can be verified using the formulas previously defined. The distance from \textbf{PP} to \textbf{MP}, here negative, is the \textbf{longitudinal aberration LAm} of the marginal rays. The beam width in the paraxial focal plane PP is the \textbf{transverse spherical aberration TSAm}, determined by the heights of the marginal rays. Notice that the smallest geometrical spot size can be found at plane \textbf{MS}, approximately 3/4 LAm back toward the lens from the paraxial focal plane. Later, this algorithmus will be used to veritfy the lens design in our simulations.

\begin{figure}[httbp]

\centering

\includegraphics[width=0.6\textwidth]{bilder/min\_max\_spot}

\caption{Schema to estimating the minimum spot location \cite{lens\_theory\_LC\_Ltd}.}

\label{fig:min\_max\_spot}

\end{figure}

This theory can be explaned by Snells Laws.

### \subsectioin{Fiber Optics}

Optical fibers are widely used as a medium for telecommuniction and networking because of varity of advantages.It is flexible,especially permits transmission over longer distances and at higher bandwidths (data rates) than other forms of communication. The Fig.\ref{fig:opticfiber} presents a simplest optical fiber and how lights progate in the fiber.

\begin{figure}[httbp]

\centering

\includegraphics[width=0.8\textwidth]{bilder/opticfiber}

\caption{linght refraction in optic fibers}

\label{fig:opticfiber}

\end{figure}

Optical fiber typically consists of a transparent core with index $n1$ surrounded by a transparent cladding material with a lower index of refraction $n2$. The Light is kept in the core by total internal reflection. This causes the fiber to act as a waveguide.

The principle of the total reflection is explained in \cite{script\_FT\_TET} with Snell's law. In Fig.\ref{fig:totalreflection} linghts strike a boundary between two different isotropic media with respective refractive indices $n\_{1}$ and $n\_{2}$ ($n\_{1}>n\_{2}$), it behaves after Snell's law, which is presented in following mathematical fomular (\ref{eq:snell}).

\begin{figure}[httbp]

\centering

\includegraphics[width=0.6\textwidth]{bilder/totalreflection}

\caption{total reflection}

\label{fig:totalreflection}

\end{figure}

\begin{equation}

n\_{1}sin\theta\_{i}=n\_{2}sin\theta\_{t}

\label{eq:snell}

\end{equation}

$\theta\_{t}$ is transmission angle or refraction angle.

At a small incidence angle $\theta\_{i1}$ a light beam can pass through the boundary and bend to a new course at transmission angle $\theta\_{t1}$ in the second meadium.

When the incidence angle is larger than a particular critical angle (\ref{eq:critical\_angle}) with respect to the normal to the surface, no light can pass through and all of the light is reflected like (O-C''). In this case the value of $sin\theta\_{t}$ in (\ref{eq:sin\_transmission\_angle}) become larger than one and he mathematical formular of the new transmission angle can be presented by a complex symble $\underline{\theta\_{t}}$(\ref{eq:complex\_transmission\_angle}). $\underline{\theta\_{t}}$ is not a real physical angle.

\begin{equation}

\theta\_{c}=arcsin(\frac{n\_{2}}{n\_{1}})

\label{eq:critical\_angle}

\end{equation}

\begin{equation}

sin\theta\_{t}=\frac{n\_{1}}{n\_{2}}sin\theta\_{i}

\label{eq:sin\_transmission\_angle}

\end{equation}

\begin{equation}

\underline{\theta\_{t}}=\frac{\pi}{2}+j\gamma

\label{eq:complex\_transmission\_angle}

\end{equation}

with

\begin{equation}

sin\underline{\theta\_{t}}=cosh\gamma=\frac{n{1}}{n\_{2}}sin\theta\_{i},\hspace{2cm}\hfill cos\underline{\theta\_{t}}=jsinh\gamma=j\sqrt{cosh^2\gamma-1}

\label{eq:trangle\_transmission\_angle}

\end{equation}

%Numerical Apertur

Back to the Fig.\ref{fig:opticfiber} the incidence beam originate from the aire into the fiber. There is a maximus coupling angle,so that the beam can be guided under the total reflecting conditions. Its sinus value(\ref{eq:NA}) is called \textbf{Numerical Apertur(NA)}, which indicate the acceptable range of ray beams.

\begin{align}

sin\theta\_{i}&=\frac{n\_{1}}{n\_{0}}sin(90^{o}-\theta\_{c})=n\_{1}cos\theta\_{c} \nonumber\\

&=n\_{1}\sqrt{1-sin^{2}\theta\_{c}}=n\_{1}\sqrt{1-\left(\frac{n\_{2}}{n\_{1}}\right)^2}=\sqrt{n^2\_{1}-n^2\_{2}}

\label{eq:NA}

\end{align}